

Structural and Magnetic Properties of (Mg, Co)₂W Hexaferrites

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Abstract: Precursor powders of BaMg_{2-x}Co_xFe₁₆O₂₇ with ($x = 0.0, 1.0$, and 2.0) were prepared using high-energy ball milling and the effects of chemical composition and sintering temperature on the structural and magnetic properties were investigated using x-ray diffractometer (XRD), scanning electron microscopy (SEM) and vibrating sample magnetometry (VSM). XRD patterns of the prepared samples indicated that crystallization of pure BaW hexaferrite phase was achieved at a sintering temperature of 1300°C , while BaM and cubic spinel intermediate phases were obtained at lower sintering temperatures of 1100°C and 1200°C . SEM images revealed an improvement of crystallization of the structural phases and a growth of the particle size with increasing the sintering temperature. The magnetic data of the samples sintered at 1300°C revealed an increase of the saturation magnetization from 59.4 emu/g to 72.6 emu/g with increasing Co concentration (x) from 0.0 to 2.0 . The coercive field H_c decreased from 0.07 kOe at $x = 0.0$ to 0.03 kOe at $x = 1.0$ and then increased to 0.09 kOe at $x = 2.0$. The thermomagnetic curves of the samples sintered at 1300°C confirmed the existence of the W-type phase and revealed spin reorientation transitions in Co-containing samples.

Keywords: W-type hexaferrites, Magnetic properties, Structural properties, Thermomagnetic measurements, Spin reorientation transition.

Introduction

Hexagonal ferrites, also known as hexaferrites, were discovered in the 1950s at Philips Research Laboratories. Since then, the degree of interest in these ferrites has been increasing exponentially due to their cost effectiveness and suitability for a wide range of industrial and technological applications [1-8]. Different types of these ferrites, the most important of which are the M-, Y-, W-, Z-, X- and U-type, were successfully synthesized and found to exhibit large variations of magnetic properties due to differences in their magnetic structures and magnetocrystalline anisotropy [2,

9-14]. Structurally, all these ferrites are hexagonal with almost the same lattice parameter $a = 5.88\text{ \AA}$ and significantly different lattice parameter c , depending on the sequence of stacking of the structural blocks (S, R, and T) in the unit cell [9, 15]. Specifically, the c -parameter for M-type barium hexaferrite with the chemical formula of BaFe₁₂O₁₉ and unit cell composed of RSR*S* stacking is typically 23.2 \AA . On the other hand, the c -parameter for W-type hexaferrite with the chemical formula BaMe₂Fe₁₆O₂₇, space group $P6_3/mmc$ and RSSR*S*S* stacking is 32.8 \AA [9, 16].

The W-type structure suggests that its unit cell can be represented by a combination of M-type unit cell and two spinel (S) structural blocks ($S = \text{Me}_2\text{Fe}_4\text{O}_8$), where the saturation magnetization can be derived from the superposition of the saturation magnetization of $M + 2S$. Accordingly, the saturation magnetization of W-type is expected to be higher than that of M-type hexaferrite of $20 \mu_B$ per formula unit (corresponding to ~ 100 emu/g) at 0 K [17]. In BaW ferrite, the additional S block has the composition $[\text{Me}_2\text{Fe}_4\text{O}_8]^0$, which is electrically neutral and has a net magnetization depending on the Me cation. For example, the experimental value of Fe_2W is $27.4 \mu_B$ (corresponding to 98 emu/g at 0 K and 78 emu/g at 293 K), which is in good agreement with the theoretical value of $28 \mu_B$. Also, the magnetic moment of Mg_2W at 0 K is expected to be equal

to that of BaM, since the magnetic moment of $\text{Mg}_2\text{Fe}_4\text{O}_8$ is theoretically zero, while the moment of Cu_2W is expected to be higher ($22 \mu_B$). The observed deviations of the experimental values from the theoretical values could be due to Me_2 ions occupying sites of the R block and performing measurements at fields lower than required for full magnetic saturation [9].

The small metal cations (Fe and Me) in W-type hexaferrite reside in seven different interstitial crystallographic sites known as $4f_{VI}$, $2d$, $12k$, $6g$, $4f$, $4f_{IV}$ and $4e$ [18, 19]. These crystallographic sites are normally grouped into five magnetic sublattices as shown in Table 1 [16, 20, 21].

TABLE 1. Crystallographic and magnetic sites and their coordinations, positions in the unit cell, net magnetic sublattice spin orientation and occupancy for BaW structure.

Magnetic site	Crystallographic site	Coordination	Block	Spin	Number of metal ions
f_{VI}	$4f_{VI}$	Octahedral	R	Down	2
a	$6g$	Octahedral	S-S	Up	3
	$4f$	Octahedral	S	Up	2
	$4e$	Tetrahedral	S	Down	2
f_{IV}	$4f_{IV}$	Tetrahedral	S	Down	2
k	$12k$	Octahedral	R-S	Up	6
b	$2d$	Bi-pyramidal	R	Up	1

Extensive research work on W-type hexaferrites prepared by different synthesis routes with a variety of cationic substitutional scenarios was carried out due to their potential for applications in microwave absorption [22-37], magnetic recording [20, 38-40] and other electrical devices [41-43]. All BaW hexaferrites, with the exception of Co_2W , are characterized by a uniaxial anisotropy. W-type hexaferrites containing Co^{2+} ions exhibit a complex magnetic structure with the variation of temperature, where spin reorientation transitions from easy plane, to easy cone, to easy axis are expected, making these ferrites of potential importance for magnetic refrigeration [24, 44-47]. Co_2W ferrite ($\text{BaCo}_2\text{Fe}_{16}\text{O}_{27}$) has a cone of easy magnetization with a constant vertex angle of 70° to the c -axis in the temperature range from -273°C to 180°C . As the temperature increases, the easy magnetization direction rotates towards the c -axis until the ferrite becomes uniaxial at 280°C [48].

Much of the research work on W-type hexaferrites available in the literature was concerned with Co- and Zn-based ferrites with a variety of cationic substitutions. Modification of the properties of the W-type ferrite based on Mg^{2+} as the divalent metal ion, however, was not addressed sufficiently in the literature [49], especially adequate structural and magnetic characterization. In this study, the effects of Co^{2+} cationic substitution for Mg^{2+} on the structural and magnetic properties of BaMg_2W hexaferrites were investigated by XRD, SEM and VSM. The results of measurements made by various experimental techniques were compared to reach an understanding of the crystalline and magnetic structure of the compounds. The spin reorientation transitions in the Co^{2+} -substituted compounds were investigated by means of thermomagnetic measurements.

Experimental

Samples of BaMg_{2-x}Co_xFe₁₆O₂₇ ($x = 0.0, 1.0$ and 2.0) were prepared by ball milling stoichiometric ratios of high purity ($\sim 99\%$) barium carbonate (BaCO₃), Fe₂O₃, CoO and MgO precursor powders using a high-energy ball mill (Fritsch Pulverisette-7) equipped with zirconia bowls and balls. The milling was carried out in an acetone medium for a period of 16 h at an angular speed of 250 rpm. The product was then left to dry in air at room temperature. Cylindrical pellets of about 1.2 cm in diameter and ~ 2 mm in thickness were made by pressing ~ 0.8 g of the powder under a 5-ton force in a stainless steel die. The discs were then sintered in an oven at 1100° C, 1200° C and 1300° C for 2 h in air.

X-ray diffraction (XRD) patterns of the sintered samples were collected using XRD 7000-Shimadzu diffractometer with Cu-K _{α} radiation ($\lambda_1 = 1.540560 \text{ \AA}$, $\lambda_2 = 1.54439 \text{ \AA}$), in the angular range $20^\circ \leq 2\theta \leq 70^\circ$ with scanning step of 0.01. The patterns were analyzed using Expert High Score 2.0.1 software to identify the structural phases and Rietveld analysis was performed for structural refinement using FullProf software.

SEM system (FEI-Inspect F50/FEG) equipped with energy dispersive spectrometer

(EDS) was used to investigate the particle morphology and size distribution, as well as the homogeneity and local chemical composition of the prepared samples. The magnetic properties of the samples were examined using vibrating sample magnetometer (VSM Micro Mag 3900, Princeton Measurements Corporation), which operated at applied fields up to 10 kOe.

Results and Discussion

XRD Results

The XRD patterns were collected in the angular range $0^\circ \leq 2\theta \leq 70^\circ$ for all samples BaMg_{2-x}Co_xFe₁₆O₂₇ ($x = 0.0, 1.0, 2.0$) sintered at 1100° C, 1200° C and 1300° C. XRD analysis using Expert High score software revealed that all samples sintered at 1300° C consisted of a single W-type phase, whereas the samples sintered at lower temperatures were all multicomponent, consisting of BaM and cubic spinel MeFe₂O₄ (Me = Mg, Co) structural phases as demonstrated by the representative patterns in Fig. 1 for the sample with $x = 1.0$. Similar results (not shown for brevity) were obtained for the samples with different x values. These results indicated that crystallization of the W-type phase at 1300° C was preceded by the crystallization of the intermediate BaM and cubic spinel phases at lower temperatures.

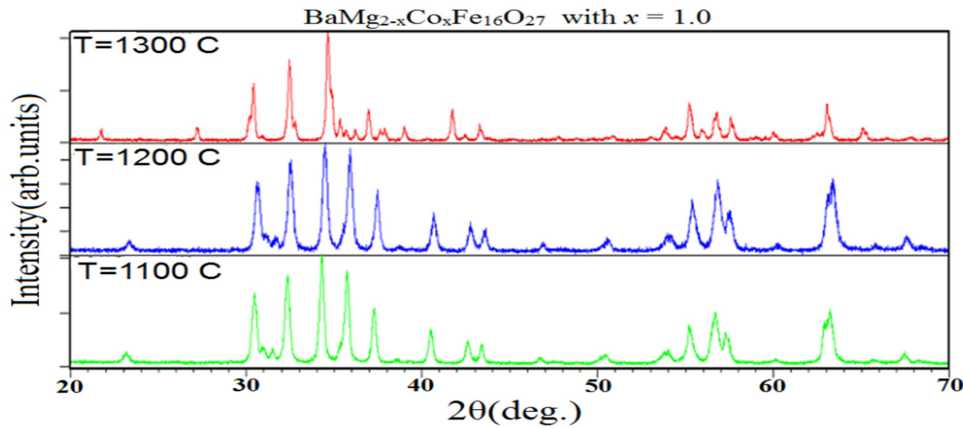


FIG. 1. X-ray diffraction patterns of BaMgCoFe₁₆O₂₇ ferrites sintered at different temperatures.

XRD pattern for the sample with $x = 2$ sintered at 1300° C revealed the existence of a single Co₂W (BaCo₂Fe₁₆O₂₇) hexaferrite phase consistent with the standard pattern (JCPDS 01-078-0135), while the patterns of the samples sintered at 1100° C and 1200° C indicated the coexistence of BaFe₁₂O₁₉ (BaM) hexaferrite phase consistent with the standard pattern (JCPDS 00-043-0002) together with CoFe₂O₄

spinel phase matching the standard pattern (JCPDS 01-079-1744). Also, the diffraction pattern for the sample with $x = 1.0$ sintered at 1300° C shows the existence of MgCo-W (BaMgCoFe₁₆O₂₇) hexaferrite phase consistent with the standard pattern (JCPDS 01-078-0135). The patterns for the samples sintered at 1100° C and 1200° C, however, indicated the existence of BaM hexaferrite phase consistent with the

standard pattern (JCPDS 00-043-0002), together with MgFe_2O_4 spinel phase consistent with the standard pattern (JCPDS 01-089-3084) and CoFe_2O_4 spinel consistent with the standard pattern (JCPDS 01-079-1744). Similarly, the XRD pattern for the sample with $x = 0.0$ sintered at 1300°C indicated the existence of a single Mg_2W ($\text{BaMg}_2\text{Fe}_{16}\text{O}_{27}$) hexaferrite phase consistent with the standard pattern (JCPDS 01-078-1551), while the patterns for the samples sintered at 1100°C and 1200°C revealed the existence of BaM hexaferrite phase consistent with the standard pattern (JCPDS 00-043-0002), together with Mg-spinel (MgFe_2O_4) phase consistent with the standard (JCPDS 01-089-3084). These results indicated that the M-phase and the spinel phase are intermediate phases that react to form the W-type phase at 1300°C .

Rietveld refinement of the XRD patterns of the samples sintered at 1300°C was performed using FullProf fitting routine (Fig. 2) and the refined lattice parameters and cell volume of the W phases are tabulated in Table 2. In Rietveld refinement, the reliability of the fit and the validity of the crystal structure model used in the fit are measured by the Bragg reliability factor

(R_B) and that of the structure factor (R_F), both of which are based on the discrepancy between the observed and calculated integrated intensities of the individual Bragg reflections. Additionally, the χ^2 parameter is a measure of the goodness of fit, which is based on the discrepancy between the observed and calculated intensities at the individual channels (angular positions). The relatively low values of these factors (Table 2) indicate reliable fit, where the structure model calculation is in good agreement with the observed diffraction data. The lattice parameters a and c for Co_2W are slightly lower than those for Mg_2W , in good agreement with previously reported results [18]. Also, the cell volume V of Co_2W is slightly ($< 0.1\%$) lower than that of Mg_2W . These results cannot be associated with the differences between the ionic radii of Mg^{2+} and Co^{2+} ions, since Co^{2+} ions have a slightly higher ionic radius at octahedral site (0.745 \AA) than Mg^{2+} (0.72 \AA) and the two ions have almost the same ionic radius at tetrahedral sites ($0.57\text{--}0.58\text{ \AA}$) [50]. Accordingly, the variations of the structural parameters can be associated with lattice distortions [5].

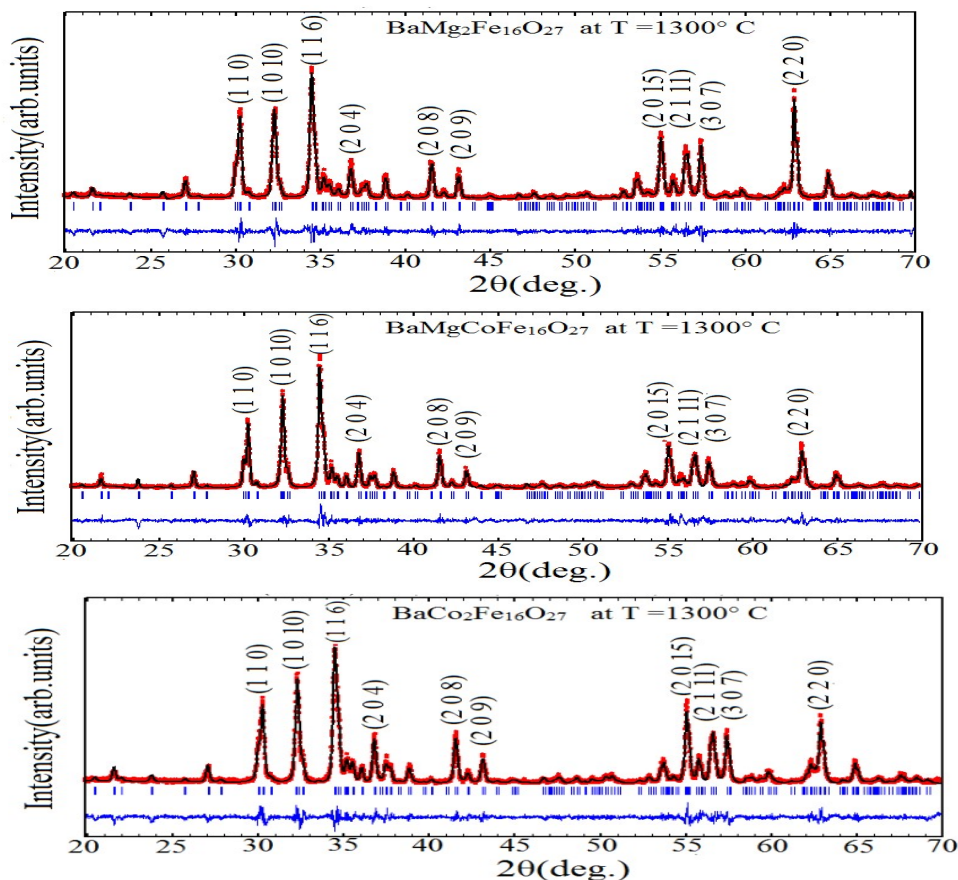


FIG. 2. Rietveld refinement of the X-ray diffraction patterns of the system $\text{BaMg}_{2-x}\text{Co}_x\text{Fe}_{16}\text{O}_{27}$ ($x = 0.0, 1.0, 2.0$) sintered at 1300°C .

TABLE 2. Results of the refinement of the patterns for the samples BaMg_{2-x}Co_xFe₁₆O₂₇ ($x = 0.0, 1.0, 2.0$) sintered at 1300° C.

Phase formula	Lattice parameters		$V (\text{\AA}^3)$	$\rho_x (\text{g/cm}^3)$	R_F	R_B	χ^2
	$a = b (\text{\AA})$	$c (\text{\AA})$					
BaMg ₂ Fe ₁₆ O ₂₇	5.9076	32.9681	996.4	5.04	1.36	1.36	1.87
BaMgCoFe ₁₆ O ₂₇	5.9061	32.9565	995.6	5.15	0.67	0.89	1.97
BaCo ₂ Fe ₁₆ O ₂₇	5.9069	32.9552	995.8	5.27	0.73	1.04	1.91

The X-ray density (ρ_x) increased linearly with increasing x , as shown in Table 2, recording an increase of 4.56% for the sample with $x = 2.0$. This increase is mainly due to the increase of the molecular weight of the W-type hexaferrite by 4.58% when Co replaced Mg completely, since the effect of the decrease of the cell volume on the X-ray density is much smaller.

The bulk density (ρ_b) of the samples sintered at 1300° C was measured by Archimedes method and the porosity (P) of each sample was evaluated using the relation:

$$P = 1 - \frac{\rho_b}{\rho_x} \quad (1)$$

The porosity of all samples (Table 3) is relatively low, indicating the possibility of producing highly densified (> 90% dense) magnets using the present synthesis route.

TABLE 3. X-ray density (ρ_x), bulk density (ρ_b) and porosity (P) of BaMg_{2-x}Co_xFe₁₆O₂₇ ($x = 0.0, 1.0, \text{ and } 2.0$) sintered at 1300° C.

x	$\rho_b (\text{g/cm}^3)$	$\rho_x (\text{g/cm}^3)$	$P (\%)$
0.0	4.72	5.04	6.4
1.0	4.75	5.15	7.7
2.0	4.82	5.27	8.5

Crystallite size (D), lattice strain and instrumental effects are the main factors that cause the broadening of the diffraction peaks [51]. The instrumental broadening must be subtracted from the observed peak broadening in order to determine the effect of the lattice strains and crystallite sizes on the peak broadening. The instrumental broadening was estimated from the broadening of the diffraction peaks of a standard silicon sample. In our study, the effect of the lattice strain was found to be very small and it could be neglected. Therefore, the only effect of the broadening of the diffraction peaks was the crystallite size.

The crystallite size was determined using the Stokes and Wilson equation [5]:

$$D = \frac{\lambda}{\beta \cos \theta} \quad (2)$$

where θ is the peak position, β is the integral breadth (= area under the peak divided by the

maximum intensity) and λ is the wavelength of radiation (1.5406 Å). The integral breadth and peak position were determined by fitting a diffraction peak with a Lorentzian line shape and the crystallite size along the corresponding crystallographic direction was evaluated. Analysis of the (1 1 0) peak at $2\theta = 30.4^\circ$ was carried out to determine the crystallite size along the basal plane of the hexagonal lattice, while analysis of the (1 0 10) peak at $2\theta = 32.4^\circ$ was performed to explore the crystallite size along the c -direction. Furthermore, the peak at $2\theta = 34.6^\circ$ was considered to explore the crystallite size in the more general direction perpendicular to the corresponding (116) crystallographic planes. The values of D for all samples along the different investigated directions revealed nanocrystalline nature for all samples with crystallite size between 32 nm and 58 nm (Table 4).

TABLE 4. The crystallite size for BaMg_{2-x}Co_xFe₁₆O₂₇ ($x = 0.0, 1.0, 2.0$) sintered at 1300° C evaluated along different crystallographic directions.

x	$D (\text{nm})$		
	(1 1 0)	(1 0 10)	(1 1 6)
0.00	36	34	35
1.00	58	57	40
2.00	30	44	32

SEM Results

SEM image of BaMg_{2-x}Co_xFe₁₆O₂₇ with $x = 0.0$ sintered at 1100° C (shown in Fig. 3-a) indicated that the sample consisted mostly of cuboidal particles and hexagonal platelets with an average size of around 230 nm. The particles in this sample seem to agglomerate with relatively high inter-particle porosity. Also, SEM image of BaMg_{2-x}Co_xFe₁₆O₂₇ with $x = 0.0$ sintered at 1200° C (Fig. 3-b) indicated that the sample consisted of cuboidal particles and hexagonal platelets with a relatively wide distribution of particle size mostly in the range between 0.2-1.0 μm . The particles in this sample stacked with low inter-particle porosity.

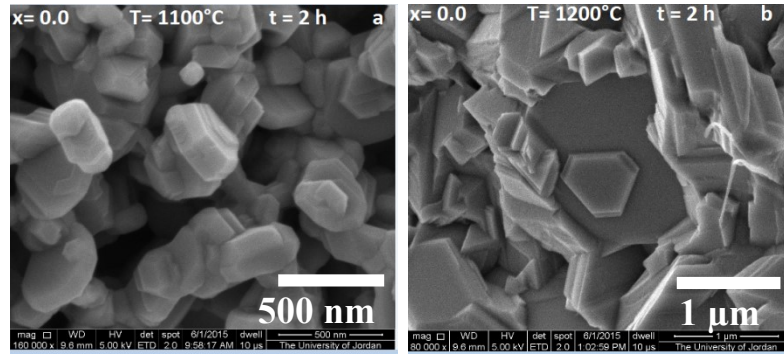


FIG. 3. SEM images of $\text{BaMg}_{2-x}\text{Co}_x\text{Fe}_{16}\text{O}_{27}$ with $x = 0.0$ sintered at (a) 1100°C and (b) 1200°C .

Representative SEM images of $\text{BaMg}_{2-x}\text{Co}_x\text{Fe}_{16}\text{O}_{27}$ with $x = 0.0$ sintered at 1300°C (Fig. 4) revealed granular structure mainly composed of regular hexagonal plates characterized by a wider distribution of particle size. The diameters of the hexagonal plates ranged between $0.7\text{--}5\text{ }\mu\text{m}$ with an average grain

size of $2.2\text{ }\mu\text{m}$. Since the critical single-domain size in hexaferrite was reported to be $0.46\text{ }\mu\text{m}$ [52], we may conclude that the sample consists of multi-domain particles. The particles in this sample stacked closely with relatively low porosity.

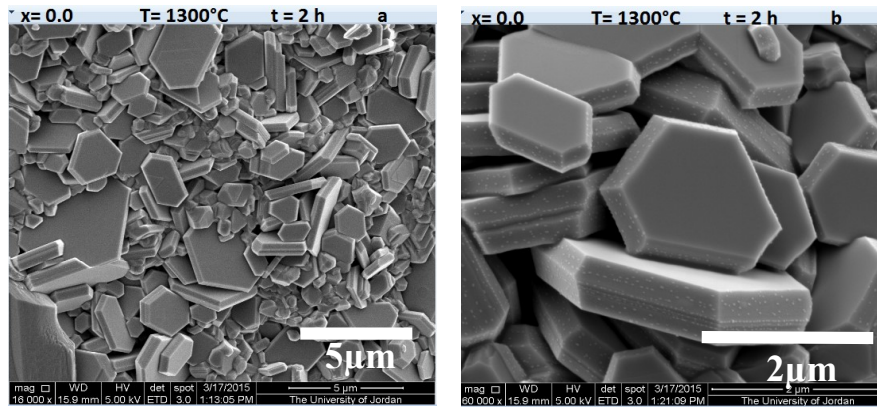


FIG. 4. SEM images of $\text{BaMg}_{2-x}\text{Co}_x\text{Fe}_{16}\text{O}_{27}$ with $x = 0.0$ sintered at 1300°C .

SEM image of $\text{BaMg}_{2-x}\text{Co}_x\text{Fe}_{16}\text{O}_{27}$ with $x = 1.0$ sintered at 1100°C (Fig. 5-a) also indicated that the sample consisted mainly of cuboidal particles and hexagonal platelets with diameters ranging between $100\text{--}500\text{ nm}$. Improvement of the crystallization of hexagonal platelets and

increase of the particle size to the range of $0.5\text{--}1.7\text{ }\mu\text{m}$ was observed at a sintering temperature of 1200°C (Fig. 5-b). Most of the particles in this sample are below the critical single domain size of about $0.5\text{ }\mu\text{m}$ and a small fraction is $> 1.0\text{ }\mu\text{m}$ in size.

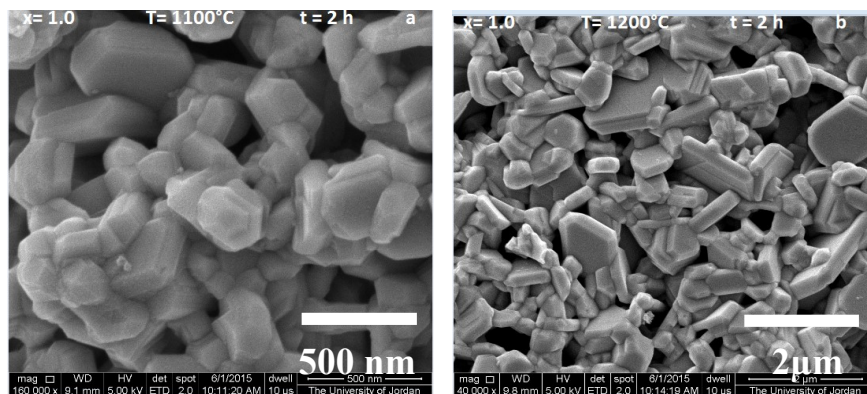


FIG. 5. SEM images of $\text{BaMg}_{2-x}\text{Co}_x\text{Fe}_{16}\text{O}_{27}$ with $x = 1.0$ sintered at (a) 1100°C and (b) 1200°C .

Fig. 6 shows representative SEM images of BaMg_{2-x}Co_xFe₁₆O₂₇ with $x = 1.0$ sintered at 1300° C. The sample is generally composed of

non-granular mass, with only a small fraction of hexagonal plates. The diameters of the hexagonal plates were between 1-3 μ m.

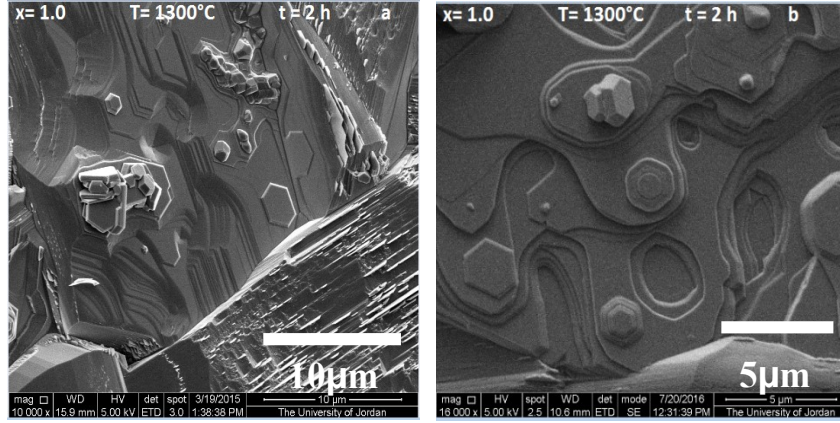


FIG. 6. SEM images of BaMg_{2-x}Co_xFe₁₆O₂₇ with $x = 1.0$ sintered at 1300° C.

In addition, SEM images (Fig. 7) of BaMg_{2-x}Co_xFe₁₆O₂₇ with $x = 2.0$ sintered at 1100° C indicated that the sample consisted mainly of cuboidal particles and hexagonal platelets with a relatively narrow distribution of particle size and

an average size of around 240 nm. The sample sintered at 1200° C (Fig. 7-b) indicated improved crystallization of hexagonal particles and the existence of large non-particulate masses.

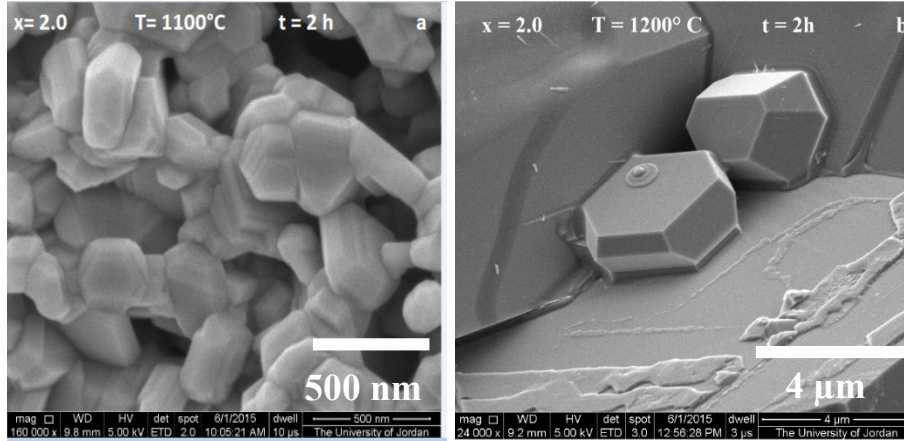


FIG. 7. SEM images of BaMg_{2-x}Co_xFe₁₆O₂₇ with $x = 2.0$ sintered at (a) 1100° C and (b) 1200° C.

Fig. 8 shows SEM images of the BaMg_{2-x}Co_xFe₁₆O₂₇ with $x = 2.0$ sintered at 1300° C. The sample is generally composed of large non-granular masses, with only a small fraction of

perfect hexagonal plates, the diameters of which were in the range of 0.5-2 μ m. The non-granular masses developed in layered, nonporous structures.

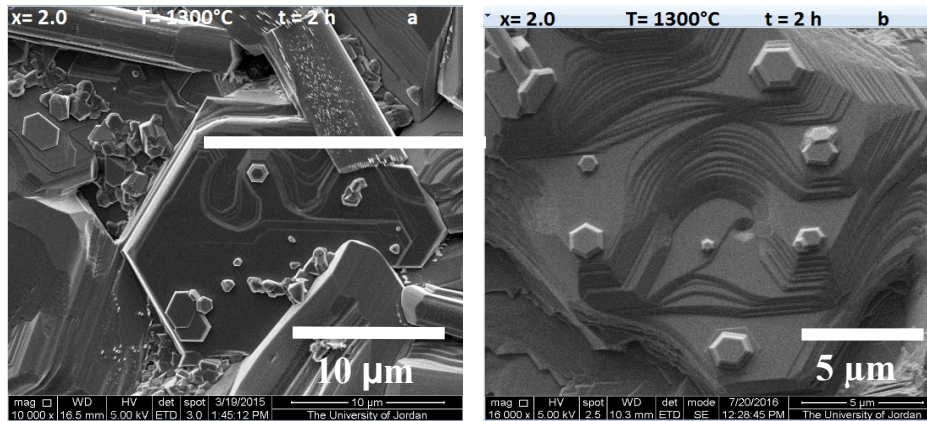


FIG. 8. SEM images of BaMg_{2-x}Co_xFe₁₆O₂₇ with $x = 2.0$ sintered at 1300° C.

Energy dispersive x-ray spectroscopy (EDS) was used to examine the chemical composition of the samples sintered at 1300° C. The spectra collected from two different spots of the sample with $x = 0.0$ revealed that the Fe:Ba ratio was 14.9 and 16.3, while the Mg:Ba ratio was 1.26 and 1.52. The Fe:Ba ratio is consistent with the theoretical stoichiometric ratio of 16.0 for Mg_2W hexaferrite, while the difference between the observed Mg:Ba ratio and the theoretical ratio of 2 cannot be accounted for by the calculated experimental uncertainty (of $\sim 20\%$). This discrepancy could be associated with the low signal for Mg and the position of its emission line in a sloped and noisy region of the background, which makes the line intensity evaluated by the software unreliable.

EDS spectra from two different spots of the sample with $x = 1.0$ indicated that the Fe:Ba ratio was 15.7 and 14.0, which is consistent with the theoretical value within the experimental uncertainty of $\sim 17\%$. The Mg:Ba ratio at the two spots was 1.95 and 0.98. Although the ratio from the second spot was in good agreement with the theoretical value of 1.00, the significantly higher value from the first spot may indicate unreliability of the evaluated Mg:Ba ratio due to the weak signal of Mg occurring in a rather noisy and sloped background. On the other hand, the Co:Ba ratio at the two spots was 2.58 and 2.06, which is more than double the theoretical value of 1.00. This difference cannot

be accounted for by the experimental uncertainty of $\sim 19\%$ and the observed high Co:Ba ratio can be attributed to the overlapping between the Co-K_α line (which was used for evaluation of the Co concentration) and the Fe-K_β spectral line (the difference of the energies of these two lines is $< 2\%$).

EDS spectrum collected from a representative point in the sample with $x = 2.0$ revealed that Fe:Ba = 15.6, which is in good agreement with the theoretical value of 16.0. On the other hand, Co:Ba ratio was found to be 3.86, which is significantly higher than the theoretical value of 2.00. Again, this high value is associated with the apparent increase of the spectral intensity of the Co-K_α line due to overlapping with Fe-K_β spectral line.

VSM Results

Room Temperature Hysteresis Loop

In this section, the magnetic properties of the system $\text{BaMg}_{2-x}\text{Co}_x\text{Fe}_{16}\text{O}_{27}$ ($x = 0.0, 1.0, \text{ and } 2.0$) samples sintered at 1100° C, 1200° C and 1300° C were investigated using room temperature hysteresis loop (HL) measurements in an applied field up to 10 kOe. The hysteresis loops (HLs) for all the samples are shown in Figs. 9, 10 and 11. The values of the saturation magnetization, M_s , remanence magnetization, M_r , and coercive field, H_c were determined from the hysteresis loops.

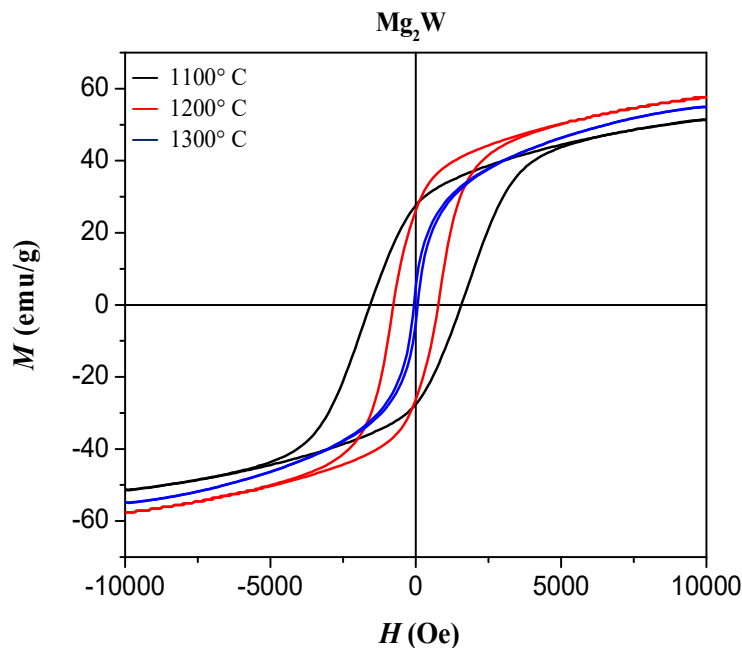
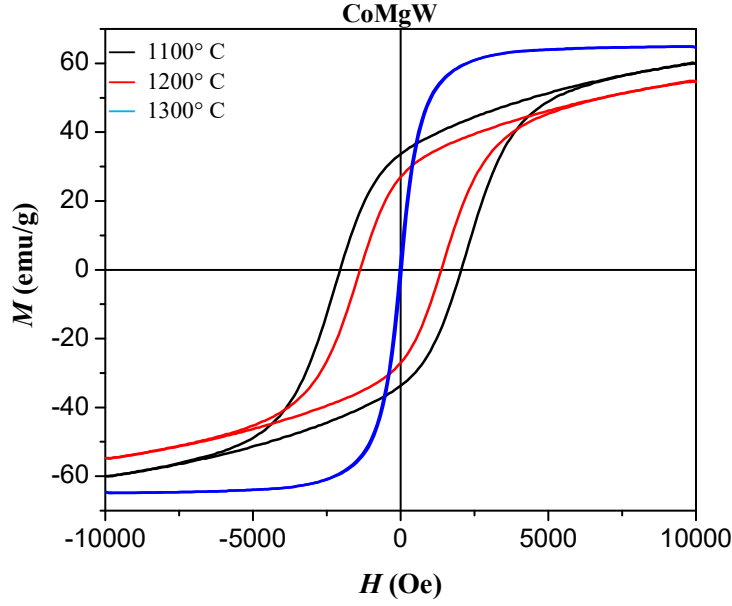
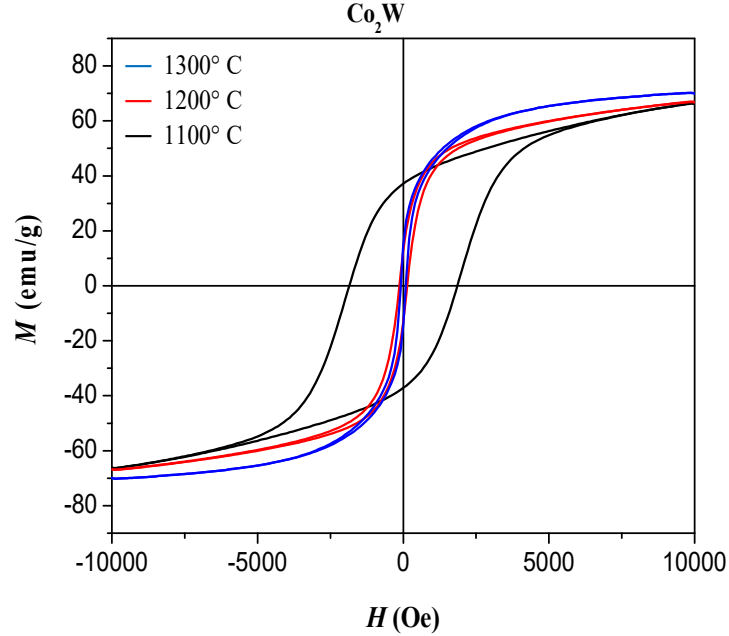


FIG. 9. Hysteresis loops of $\text{BaMg}_{2-x}\text{Co}_x\text{Fe}_{16}\text{O}_{27}$ with $x = 0.0$ sintered at 1100° C, 1200° C and 1300° C.

FIG. 10. Hysteresis loops of BaMg_{2-x}Co_xFe₁₆O₂₇ with $x = 1.0$ sintered at 1100° C, 1200° C and 1300° C.FIG. 11. Hysteresis loops of BaMg_{2-x}Co_xFe₁₆O₂₇ with $x = 2.0$ sintered at 1100° C, 1200° C and 1300° C.

The HLs for all samples indicated magnetic softening with the increase of the sintering temperature. The coercivity and remanence magnetization were determined directly from the hysteresis loops, while the saturation magnetization, M_s , was determined from the law of approach to saturation (LAS) [12, 53]:

$$M = M_s \left(1 - \frac{A}{H} - \frac{B}{H^2} \right) + \chi H \quad (3)$$

Here, M is the magnetization (in emu/cm³), M_s is the spontaneous saturation magnetization of the domains per unit volume, A is a constant associated with microstress and/or inclusions, B

is a constant representing the magnetocrystalline anisotropy contribution and χH is the forced magnetization term. Plotting M versus $1/H^2$ in the high field range 8.5 – 10 kOe gave straight lines, indicating that the magnetization in this field range is determined completely by the magnetocrystalline term.

The saturation magnetization was determined from the intercept of the straight line with the M -axis. The magnetic parameters derived from the hysteresis loops are tabulated in Table 5.

TABLE 5. Saturation magnetization, remanence magnetization, squareness ratio and coercive field for $\text{BaMg}_{2-x}\text{Co}_x\text{Fe}_{16}\text{O}_{27}$ sintered at different temperatures.

x	$T(^{\circ}\text{C})$	$M_s(\text{emu/g})$	$M_r(\text{emu/g})$	M_{rs}	$H_c(\text{kOe})$
0.0	1100	55.4	27.5	0.50	1.57
0.0	1200	62.1	26.1	0.42	0.77
0.0	1300	59.4	4.33	0.07	0.07
1.0	1100	64.5	33.6	0.52	2.05
1.0	1200	59.8	26.9	0.45	1.37
1.0	1300	65.2	2.66	0.04	0.03
2.0	1100	72.6	37.1	0.51	1.85
2.0	1200	71.2	12.1	0.17	0.14
2.0	1300	72.6	11.7	0.16	0.09

Because the W-type hexaferrite structure is built up of M-type hexaferrite and S block, where S block contains two spinel molecules, the magnetic moment of the W-type hexaferrite can be described by the relations [9, 34, 54],

$$\mu_W = \mu_M + 2\mu_S, \quad (4)$$

$$\mu = \frac{MM_s}{N_A\mu_B}, \quad (5)$$

where μ_M is the magnetic moment of $\text{BaFe}_{12}\text{O}_{19}$ and μ_S is the magnetic moment of spinel, M is molecular weight, M_s is the saturation magnetization, N_A is Avogadro's number (6.023×10^{23} molecules/mole), μ_B is the Bohr magneton (9.27×10^{-21} erg/G) and μ is the magnetic moment of a given compound. Therefore, by combining Eq. (4) and Eq. (5), we obtain:

$$(M_s)_W = \left[\frac{M_M}{M_W} \right] (M_s)_M + 2 \left[\frac{M_S}{M_W} \right] (M_s)_S. \quad (6)$$

This last equation predicts that the saturation magnetization of Mg_2W is 58.6 emu/g, which is in good agreement with the observed value of 59.4 emu/g for Mg_2W sample sintered at 1300° C. On the other hand, the expected theoretical saturation magnetization of MgCoW is 66 emu/g, which is also in good agreement with the observed value of 65.2 emu/g. Further, the expected saturation magnetization of Co_2W is 72.96 emu/g, which is also in good agreement with the observed value of 72.6 emu/g. These results indicate that the magnetization of the W-type phase can be determined from the superposition of the magnetizations of the underlying magnetic phases.

The saturation magnetization for the sample with $x = 0$ increased with sintering temperature from 55.4 emu/g for the sample sintered at 1100° C to 62.1 emu/g for the sample sintered at 1200° C. The sample sintered at 1100° C is a mixture

of BaM phase and MgFe_2O_4 phase, as indicated by XRD analysis. Assuming that the magnetization of the sample results from a simple superposition of the BaM and Mg-spinel phases and using the values of the saturation magnetizations of polycrystalline BaM phase of 70 emu/g [1] and of 27 emu/g for MgFe_2O_4 phase [9], the saturation magnetization for the sample sintered at 1100° C (55.4 emu/g) suggests that this sample is composed of about 66 wt. % BaM phase and 34 wt. % MgFe_2O_4 phase. If all Mg were incorporated in the formation of MgFe_2O_4 spinel phase, the sample would consist of BaM and Mg-spinel phase with a molar ratio of 1:2, corresponding to 73.5 wt.% BaM and 26.5 wt.% Mg-spinel (molar mass of Mg-spinel = 200 g and of BaM = 1111.5 g). These fractions should give a theoretical value of 58.6 emu/g, which is higher than the observed value. The lower observed value could then be attributed to BaM and Mg-spinel phases with saturation magnetizations lower than the theoretical values. The saturation magnetization results are therefore consistent with the picture of phase segregation into BaM and Mg-spinel at a sintering temperature of 1100° C. The saturation magnetization of the sample sintered at 1200° C (62.1 emu/g), on the other hand, suggests that the sample consists of about 81.6 wt. % of BaM phase and 18.4 wt. % of MgFe_2O_4 phase. This may indicate that a fraction of the Mg ions substitutes Fe ions in the hexaferrite phase, which results in a reduction of the mass fraction of the Mg-spinel in the sample and a consequent increase of the saturation magnetization.

The coercivity of the samples with $x = 0$ decreased from 1.57 kOe for the sample sintered at 1100° C, down to 0.77 kOe at a sintering temperature of 1200° C and to 0.07 kOe at a

sintering temperature of 1300° C. The decrease of the coercivity of the sample sintered at 1200° C can be attributed to the significant increase of the particle size as the temperature increases (SEM results). The significant drop in the coercivity of the sample sintered at 1300° C is associated with the crystallization of large hexagonal plates of Mg₂W phase by solid state reaction of the intermediate BaM and MgFe₂O₄ phases at high sintering temperatures. The decrease of the squareness ratio (M_{rs}) to values below 0.5 (which is characteristic of single-domain, randomly oriented assembly of particles) is consistent with particle growth to the multidomain particle size regime. The multidomain nature of the particles is responsible for the significant decrease in coercivity, since in this case, the domain-wall motion is dominant in the magnetization processes.

The saturation magnetization for the sample with $x = 1$ decreased from 64.5 emu/g for the sample sintered at 1100° C, down to 59.8 emu/g at a sintering temperature of 1200° C, then increased up to 65.2 emu/g at a sintering temperature of 1300° C. The sample sintered at 1100° C is a mixture of BaM phase and MgFe₂O₄ and CoFe₂O₄ spinel phases. Again, assuming that the saturation magnetization of the sample sintered at 1100° C results from a simple superposition of the saturation magnetizations of the magnetic phases in the sample and using the saturation magnetization of 80 emu/g for CoFe₂O₄ phase [9], the saturation magnetization for this sample (64.5 emu/g) is consistent with 62 wt. % of BaM phase, 17.5 wt. % of MgFe₂O₄ phase and 20.5 wt. % of CoFe₂O₄ phase. In calculating the weight fractions, the ratio of the molar mass of Co-spinel to that of Mg-spinel (1.173) and equal molar ratios of the two spinel phases were assumed to determine the fractions of the two spinel phases. The relative weight fractions of the BaM and spinel phases (62 wt. % and 38 wt. %, respectively) are similar to those of the sample with $x = 0$ sintered at the same temperature. The saturation magnetization of the sample sintered at 1200° C decreased to 59.8 emu/g, which is consistent with 30 wt.% BaM, 32.2 wt.% Mg-spinel and 37.8 wt.% Co-spinel. The increase of the weight fraction of the spinel phases (the weighted average of saturation magnetization of which is 55.6 emu/g) cannot be justified on the basis of the starting materials in the sample and therefore, the reduction of the

saturation magnetization could be attributed to the presence of BaM and spinel phases with saturation magnetizations lower than their theoretical values.

The sample sintered at 1300° C is composed of MgCo-W hexaferrite. The increase in saturation magnetization with respect to the sample with $x = 0.0$ can be associated with the increase of the magnetic moment per molecular formula. Since Mg²⁺ is a non-magnetic ion and the magnetic moment of Co²⁺ ion is 3.7 μ_B , the increase in the saturation magnetization of this sample suggests that Co²⁺ ions replace Mg²⁺ ions at spin-up sites.

The coercivity decreased from 2.05 kOe for the sample sintered at 1100° C, down to 1.37 kOe at a sintering temperature of 1200° C and to 0.03 kOe at a sintering temperature of 1300° C. The decrease of the coercivity of the sample sintered at 1200° C could be associated with the increase of particle size of the BaM phase. The sharp drop in the coercivity of the sample sintered at 1300° C, however, is associated with phase transformation from hard BaM phase to soft BaW phase with large particle size. The small decrease of the squareness ratio, M_{rs} , from 0.52 for the sample sintered at 1100° C to 0.45 for the sample sintered at 1200° C is consistent with the small increase of the particle size beyond the critical single domain size as indicated by SEM images. The sharp drop in the squareness ratio down to 0.04 for the sample sintered at 1300° C, however, is due to transformation from hard BaM magnetic phase with almost single-domain particle size to soft, large non-granular masses of BaW phase.

The saturation magnetization for the samples with $x = 2$ revealed similar values at the different sintering temperatures (72.6 emu/g for the sample sintered at 1100° C, 71.2 emu/g at a sintering temperature of 1200° C and 72.6 emu/g at a sintering temperature of 1300° C). The sample sintered at 1100° C is a mixture of BaM and CoFe₂O₄ as indicated by XRD analysis. The saturation magnetization of 72.6 emu/g is consistent with 74 wt. % BaM and 26 wt. % CoFe₂O₄. If we assume that Co²⁺ ions were fully consumed in the spinel phase, the fractions of the BaM and spinel phase would be 70.3 wt.% and 29.7 wt.%, respectively, corresponding to an expected saturation magnetization of 72.96 emu/g. This value is similar to the observed saturation magnetization, which is an indication

of that this sample consists of BaM and Co-spinel phases with saturation magnetizations close to the theoretical values. On the other hand, the saturation magnetization of 71.2 emu/g for the sample sintered at 1200° C could indicate that Co partially substituted Fe in the hexaferrite lattice. The saturation magnetization of the sample sintered at 1300° C is 72.6 emu/g, which is in good agreement with the previously reported values of 71.18 emu/g for BaCo₂Fe₁₆O₂₇ [41] and 74.31 emu/g for SrCo₂Fe₁₆O₂₇ [55].

The coercivity decreased from 1.85 kOe for the sample sintered at 1100° C, down to 0.14 kOe at a sintering temperature of 1200° C and down to 0.09 kOe at a sintering temperature of 1300° C. These dramatic changes were associated with magnetic softening as a result of particle growth at 1200° C sintering temperature and the transformation of BaM and Co-spinel phases to large, non-granular masses of W-type hexaferrite phase at 1300° C sintering

temperature. The significant decreases of the squareness ratio M_{rs} from 0.51 to 0.17 and 0.16 is an indication of that the samples sintered at 1200° C and 1300° C consist of large multidomain volumes in these samples.

The soft magnetic character and the low coercivity values of 70 Oe for Mg₂W, 30 Oe for MgCo-W and 90 Oe for Co₂W for the samples sintered at the highest temperature of 1300° C are in good agreement with the values reported for Co-substituted Zn₂W ferrites [56]. The increase of the saturation magnetization from 59.4 emu/g for Mg₂W to 65.2 emu/g for CoMg-W and then to 72.6 emu/g for Co₂W is a result of the substitution of Mg²⁺ ions by Co²⁺ ions at spin-up sites. The saturation trends of the samples (Fig. 12) revealed that the magnetization of sample with $x = 1.0$ is almost saturated at an applied field of 10 kOe, indicating low magnetocrystalline anisotropy relative to the two end compounds ($x = 0.0$ and 2.0).

T = 1300° C

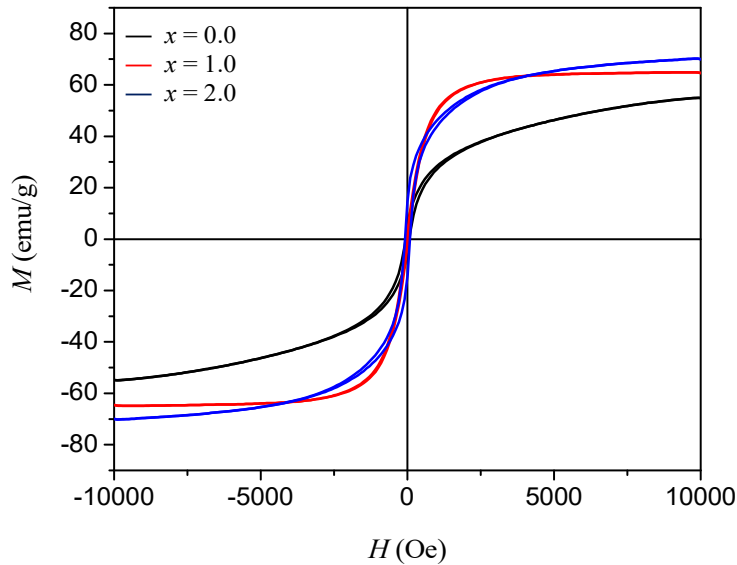


FIG. 12. Hysteresis loops of BaMg_{2-x}Co_xFe₁₆O₂₇ ($x = 0.0, 1.0$ and 2.0) sintered at 1300° C.

Thermomagnetic Measurements

The thermomagnetic curves of the system BaMg_{2-x}Co_xFe₁₆O₂₇ ($x = 0.0, 1.0$ and 2.0) sintered at 1300° C (measured at an applied field of $H = 100$ Oe) are shown in Fig. 13, together with their derivatives with respect to temperature. The derivative curves of all samples exhibited strong negative peaks (dips) at temperatures > 450 ° C, which were associated with the Curie temperature of the corresponding W-type phase as shown in Table 6. The observed Curie temperature of 452° C for Mg₂W is equal to the previously reported value of (452±3)° C

[18] and that of 483° C for Co₂W is in good agreement with the reported values of (490±3)° C [18] and (477±5)° C [46] for this compound, while the Curie temperature of 473° C for MgCo-W lies between the Curie temperatures of the end compounds. The results indicated that the Curie temperature increased with the increase of the Co content, as a consequence of the enhancement of the superexchange interactions resulting from the substitution of Mg²⁺ nonmagnetic ions by Co²⁺ magnetic ions. The occurrence of a single strong dip in the derivative curve suggests that each sample is composed of a single W-type phase.

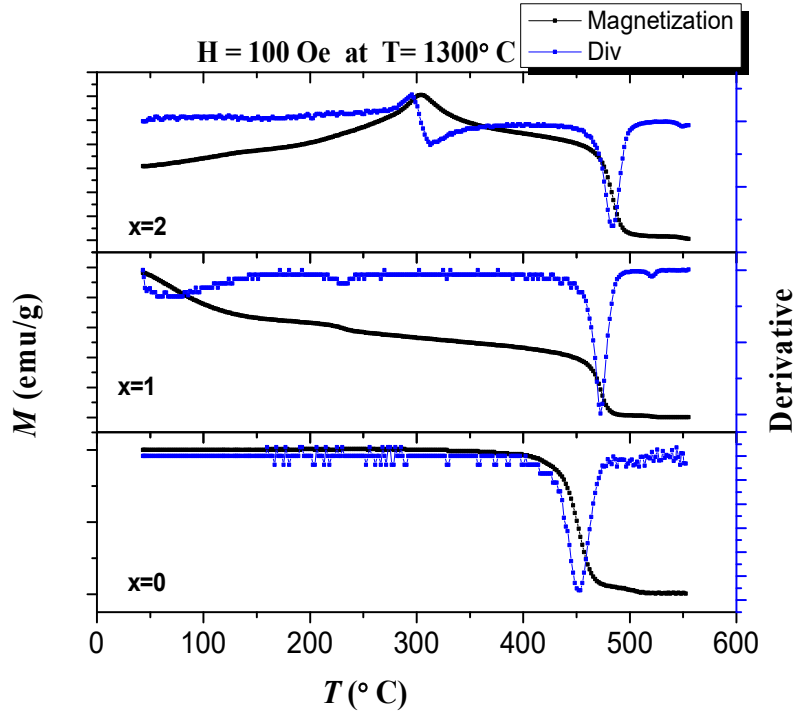


Fig. 13: Thermomagnetic curves of $\text{BaMg}_{2-x}\text{Co}_x\text{Fe}_{16}\text{O}_{27}$ ($x = 0.0, 1.0$ and 2.0) samples sintered at 1300°C .

TABLE 6. Curie temperature of the different samples $\text{BaMg}_{2-x}\text{Co}_x\text{Fe}_{16}\text{O}_{27}$ ($x = 0.0, 1.0$ and 2.0).

x	0.0	1.0	2.0
T_c ($^\circ\text{C}$)	452	473	483

The derivative curve of the sample with $x = 1.0$ shows two additional weak dips at 232°C and 522°C resulting from inflection points on the magnetization curve. The weak peak at 232°C could be associated with spin reorientation transition, where the magnetic anisotropy changes from easy-cone to easy-axis. This temperature is lower than the reported spin reorientation transition temperature for Co_2W [46, 48], which is consistent with the reported increase of the spin reorientation transition temperature with the increase of Co content in Co-substituted Zn_2W ferrite [46, 47]. Further, this result is an indication of that both Mg^{2+} and Co^{2+} ions are incorporated into a single W-type phase. The high-temperature dip at 522°C is close to the reported Curie temperature of 527°C for $\text{BaCoZn}_{0.5}\text{Mg}_{0.5}\text{Fe}_{16}\text{O}_{27}$ [57] and could be associated with traces of Co-rich magnetic impurities in our sample.

The rise in the thermomagnetic curve of the sample with $x = 2.0$ into a peak at $\sim 304^\circ\text{C}$ is associated with the spin reorientation transition from conical to c -axis spin orientation. The shape of the derivative curve around this

temperature suggests a singular-type behavior of the magnetization, indicating that the origin of the peak is not a smooth function. This behavior is associated with the competition between the rise in the magnetization due to spin reorientation transitions and the decline due to thermal agitation. The spin reorientation transition in this sample is clearly observed at a higher temperature compared with MgCo-W . Also, a weak negative peak is observed in the derivative curve at $\sim 550^\circ\text{C}$, which can be associated with the enhancement of the superexchange interactions in Co-rich regions of the sample.

Conclusions

W-type hexaferrites were synthesized by high energy ball milling and sintering at 1300°C . The hexaferrite phase evolved from the reaction of BaM hexaferrite and cubic spinel intermediates which crystallize at lower temperatures. The saturation magnetization as well as the Curie temperature of the W-type hexaferrite increased with the increase of the Co concentration. This is a consequence of the increase of the net magnetic moment per molecule upon replacement of nonmagnetic Mg^{2+} ions by magnetic Co^{2+} ions and the consequent enhancement of the superexchange interactions between magnetic ions in spin-up and spin-down sublattices. The observed saturation

magnetization of the W-type phase in all samples was in good agreement with the calculated value using a model involving the superposition of cubic spinel and M-type ferrite phases, indicating that Mg^{2+} and Co^{2+} ions occupy octahedral sites corresponding to the (a) spin-up magnetic sublattice in the spinel (S) blocks of

the W-type unit cell. The thermomagnetic curves of the W-hexaferrites revealed spin reorientation transition around room temperature in the sample with $x = 2.0$, which could be of potential importance for magnetic refrigeration applications.

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